

**(1) [5 points]** See the textbook (Section 8.6) for a discussion of Section 2 of the Sherman Act (1890). The most relevant part is “attempting to monopolize.”

**(2) [10 points]** Because

$$e_a = \frac{\% \Delta q}{\% \Delta a} = 0.04 \quad \text{and} \quad e_p = \frac{\% \Delta q}{\% \Delta p} = -0.2,$$

by the Dorfman-Steiner formula the profit-maximizing ratio of advertising expenditure to sales revenue is given by

$$\frac{A}{pq} = \frac{A}{\$50 \text{ million}} = \frac{1}{5} = \frac{0.04}{-(-0.2)} = \frac{e_a}{-e_p}.$$

Hence,  $A = \$10$  million.

**(3a) [10 pts.]** Setting a high price for CNN,  $p_C = \$11$ , results in 200 subscribers, hence a profit of  $\pi_C = (11 - 1)200 = \$2000$ . Setting a low price,  $p_C = \$2$ , results in 400 subscribers, hence a profit of  $\pi_C = (2 - 1)400 = \$400$ . Therefore,  $p_C = \$11$  is profit maximizing. Similarly, BBC subscriptions should also be sold for  $p_B = \$11$ .

Setting a high price for HIS,  $p_H = \$6$ , results in 200 subscribers, hence a profit of  $\pi_H = (6 - 1)200 = \$1000$ . Setting a low price,  $p_H = \$3$ , results in 400 subscribers, hence a profit of  $\pi_H = (3 - 1)400 = \$800$ . Therefore,  $p_H = \$6$  is the profit-maximizing price. Altogether, the total profit under no tying is  $\pi^{NT} = 2000 + 2000 + 1000 = \$5000$ .

**(3b) [10 pts.]** Setting a high package price,  $p_{CBH} = \$19$ , results in 200 subscribers, hence a profit of  $\pi^{PT}(19) = (19 - 3)200 = \$3200$ . Setting a low price,  $p_{CBH} = \$16$ , results in 400 subscribers, hence a profit of  $\pi^{PT}(16) = (16 - 3)400 = \$5200$ . Therefore,  $p_{CBH} = \$16$  is the profit-maximizing price.

**(3c) [5 pts.]** Suppose now that the cable TV operator makes the following offer: Viewers can subscribe to a “news” package containing CNN and BBC for a price of  $p_{CB} = \$13$  and the HIS(tory) channel for  $p_H = \$6$ . Inspecting the table reveals that all 400 consumers will subscribe to the “news” package whereas only 200 will subscribe to the HIS(tory) channel. Hence, total profit under mixed tying is

$$\pi^{MT} = (13 - 2)400 + (6 - 1)200 = \$5400 > \pi^{PT} = \$5200 > \pi^{NT} = \$5000.$$

Therefore, mixed tying is more profitable than either pure tying or no tying.

**(4a) [10 points]** If summer turns out to be the peak season, the airline should solve

$$\begin{aligned} MR_S(q_S) = 36 - q_S &= \$2 + \$4 = c + r, & \implies q_S^{pl} = k^{pl} = 30 \\ MR_W(q_W) = 36 - 2q_W &= \$2 = c, & \implies q_W^{pl} = 17 < k^{pl}. \end{aligned}$$

Therefore,  $p_S^{pl} = \$21$  and  $p_W^{pl} = \$19$ .

**(4b)[10 points]** Let  $p = p_W = p_S$ . In this case, the direct demand functions are:

$$q_S = 2(36 - p) > q_W = 36 - p, \quad \text{for all } p \geq 0.$$

The seller solves

$$\begin{aligned} \max_p \pi(p) &= p(q_W + q_S) - (2 + 4)q_S - 2q_W \\ &= p[2(36 - p)] + p(36 - p) - (2 + 4)[2(36 - p)] - 2(36 - p) = -3p^2 + 122p - 504. \end{aligned}$$

The first-order condition yields  $0 = d\pi/dp = 122 - 6p$ . The second-order condition for a maximum is satisfied since  $d^2\pi/dp^2 = -6 < 0$ . Therefore,  $p_{S,W} = 61/3 \approx \$20.33$ .

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**(5a) [5 points]**  $p^{NW} = \rho V = 0.8 \cdot 40 = \$32$ .  $\pi^{NW} = \rho V - c = 0.8 \cdot 40 - 10 = \$22$

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**(5b) [10 points]**  $p^{FW} = V = \$40$ .

$$\pi^{FW} = p^{FW} - \frac{c}{\rho} = 40 - \frac{10}{0.8} = \frac{320 - 100}{8} = \frac{55}{2} = \$27.5.$$


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**(5a) [5 points]**

$$p^{PW} = \rho V + (1 - \rho)20 = 0.8 \cdot 40 + 0.2 \cdot 20 = \$36.$$

Therefore, the profit is

$$\pi^{PW} = p^{PW} - c - (1 - \rho)20 = 36 - 10 - 0.2 \cdot 20 = \$22 = \pi^{NW}.$$

Hence, this type of warranty yields the same profit as with no warranty.

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**(6) [20 points] Option A:** The probability that both labs do not discover is:  $(1 - 0.75)^2 = 1/16$ . Therefore, expected profit is given by

$$\pi = \left(1 - \frac{1}{16}\right) 16 - 2 \cdot 2 = \$11.$$

**Option B:** The probability that all three labs do not discover is:  $(1 - 0.5)^3 = 1/8$ . Therefore, expected profit is given by

$$\pi = \left(1 - \frac{1}{8}\right) 16 - 3 \cdot 1 = \$11.$$

Therefore, both options yield the same expected profit.

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**THE END**